Integration of feedforward neural network and finite element in the draw-bend springback prediction

M.R. Jamli a,b,⁎, A.K. Ariffin c, D.A. Wahab a

a Department of Mechanical and Materials Engineering, Faculty of Engineering and Built Environment, Universiti Kebangsaan Malaysia, 43600 UKM Bangi, Selangor, Malaysia
b Department of Manufacturing Process, Faculty of Manufacturing Engineering, Universiti Teknikal Malaysia Melaka, Hang Tuah Jaya, 76100 Durian Tunggal, Melaka, Malaysia

c Department of Manufacturing Process, Faculty of Manufacturing Engineering, Universiti Teknikal Malaysia Melaka, Hang Tuah Jaya, 76100 Durian Tunggal, Melaka, Malaysia

A R T I C L E   I N F O

Keywords:
Finite element
Neural network
Nonlinear elastic recovery
Springback prediction

A B S T R A C T

To achieve accurate results, current nonlinear elastic recovery applications of finite element (FE) analysis have become more complicated for sheet metal springback prediction. In this paper, an alternative modelling method able to facilitate nonlinear recovery was developed for springback prediction. The nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-nonlinear elastic recovery was processed using back-propagation networks in an artificial neural network (ANN). This approach is able to perform pattern recognition and create direct mapping of the elastically-

1. Introduction

Sheet metal forming has been used widely in the manufacturing industry, especially in the automotive manufacturing sector. One of the main problems faced in the sheet metal forming process is the springback phenomenon. The occurrence of springback after the formation process results in inaccuracy of the final dimensions for a particular product. For decades, springback prediction techniques have been studied using the finite element (FE) method to replace the testing (trial and error) procedure in order to reduce the time and cost of analysis. Prediction by the FE method requires a deep knowledge of several factors that influence the final result of the analysis such as the friction coefficient, mesh density, material constitutive model, and so on. The material constitutive model is one of the most important factors that influence the accuracy of sheet metal springback prediction by the FE method (Eggertsen & Mattiasson, 2011). Although proper utilisation of yield criteria and hardening laws is essential to accurately reproduce the material flow stress, the accuracy of the simulation of elastic unloading behaviour remains a significant factor for the end result of sheet metal springback. This is due to the nonlinearity of elastic unloading that occurs during the springback process after the forming load is released from the metal strips.

The development of an additional surface in the yield surface (Eggertsen & Mattiasson, 2010b) and the transition of the elastic to the plastic model (Quasi-Plastic–Elastic model) (Sun & Wagoner, 2011) have been proposed for the description on nonlinear elastic recovery in constitutive modelling. However, due to the complexity of developing the nonlinear recovery model, the variable elastic modulus achieves a relatively wider range of application in springback predictions (Chatti & Hermi, 2011; Zhu, Liu, Yang, & Li, 2012).

An artificial neural network (ANN) is a mathematical model that attempts to mimic the large amount of interconnections of the biological neurons in the human brain to perform a complex processing task. The behaviour of complex experimental data can be predicted by developing a neural network model with sufficient input data. In the past years, the applications of ANN in the field of sheet metal forming have been used as inverse techniques by utilising FE analysis to predict parameters for established constitutive models. Aguir, BelHadjSalah, and Hambli (2011) proposed a hybrid optimization strategy based on an FE method, ANN computation, and genetic algorithm (GA) to identify the Karafillis and Boyce criterion, and the Voce law hardening parameters. Aguir, Chamkeh, BelHadjSalah, Dogui, and Hambli (2008) used ANN to identify the parameters which reduce the difference between the FE method and the experimental measurements. Veera Babu, Ganesh Narayanan, and Saravana Kumar (2010) developed an ANN model to predict the deep drawing behaviour using a large set of data from simulation trials. Kazan, Firat, and Tiryaki (2009) investigated springback in the wipe-bending process, developing an ANN model based on data obtained from FE analysis.

Instead of utilising FE to provide training data, ANN models have also been used for mapping input and output parameters based on a large set of experimental measurements. Baseri, Bakhshi-Jooybari, and Rahmani (2011) proposed a new fuzzy...
learning back-propagation (FLBP) algorithm to predict the springback. The model was trained using the data generated based on experimental observations. Narayanasamy and Padmanabhan (2010) compared regression modelling and ANN for predicting springback in a steel sheet. In other metal-forming fields, there are several reports on the application of ANN to model complex constitutive models without any implementation of ANN-based constitutive models in FE code (Ji, Li, Li, Li, & Li, 2010; Jing, 2011; Lin, Zhang, & Zhong, 2008; Lu et al., 2011; Sun et al., 2010; Toros & Ozturk, 2011; Zhu, Zeng, Sun, Feng, & Zhou, 2011).

The disadvantages of the FE inverse technique are that the end results are limited to the FE code capability, and a large number of simulation data are required. On the other hand, ANN prediction that is based on experimental measurements cannot be used in the FE simulation. At the same time, a large number of experimental data are required, resulting in a high experimental cost. These problems can be solved by utilising ANN as a constitutive model or a part of it in an FE analysis. In the wide engineering spectrum, several researchers have implemented it in their works (Haj-Ali & Kim, 2007; Yun, Ghaboussi, & Elshah, 2008a; Yun, Ghaboussi, & Elshah, 2008b). Jung and Ghaboussi (2006) reported the formulation of a rate-independent ANN-based material model for concrete and its implementation in FE software through a user-defined material subroutine (Abaqus-UMAT). Kessler, El-Gizawy, and Smith (2005) developed an ANN based material model for 6061 aluminium in the FE analysis of metal forging process through a user-defined material subroutine (Abaqus-VUMAT). Despite these applications, the technique has not yet been applied in the nonlinear recovery of sheet metal springback.

The objective of this paper is to develop a model that can predict the nonlinear elastic recovery through a soft computing approach, and that will be practically useful as part of a material constitutive model in FE analysis. In the present work, an ANN model is developed to predict the relationship of the nonlinear unloading modulus after a range of plastic pre-strains. The trained network model is integrated with the FE code through a user-material subroutine. The accuracy of the present work was validated with simulation results of the draw-bend springback test.

2. Principle of nonlinear elastic recovery

Most of the current FE method practises still utilise classic elasto-plasticity theory, which assumes that the unloading modulus after plastic deformation is parallel to the initial Young’s modulus ($E_0$). However, several investigations have shown that the unloading modulus is influenced by accumulated plastic strain (Andar, Kuwabara, Yonemura, & Uenishi, 2010; Cleveland & Ghosh, 2002; Eggertsen & Mattiasson, 2009a, 2009b, 2010a, 2010b, 2010c; Yoshida, Uemori, & Fujiwara, 2002). A decreasing unloading modulus with increasing pre-strain can be observed with a given saturated value after a large pre-strain is applied. The degradation of the unloading modulus with respect to the plastic pre-strain is represented by an exponential formula which is known as the chord modulus ($E_{av}$). This formula was further used by several studies to produce more accurate springback prediction results (Chatti, 2010; Eggertsen & Mattiasson, 2009a, 2009b, 2010a, 2010b, 2010c; Yoshida & Uemori, 2003; Yu, 2009). Although $E_{av}$ has been widely used by many researchers, several investigations have found that the unloading stress–strain curve actually shows nonlinear elastic recovery (Andar et al., 2010; Cleveland & Ghosh, 2002; Cáceres, Sumitomo, & Veidt, 2003).

Fig. 1 shows the nonlinear unloading stress–strain curve with respect to $E_0$ and $E_{av}$. After plastic deformation to point A, the unloading process begins at point A and ends at point C according to $E_0$, which describes the linear elastic recovery. On the other hand, the application of $E_{av}$ results in point B as the end of the unloading process. However, the nonlinear curve AB is the actual unloading path that describes nonlinear recovery. To obtain an accurate springback prediction, the simplification of the nonlinear recovery is inadequate if the springback phase achieves a relaxation in the total stresses. Nevertheless, generally at the end of the springback phase, the stresses produced in the forming phase decrease but remain as residual stresses, which confirms the requirement for nonlinear recovery modelling in springback predictions (Eggertsen & Mattiasson, 2010b).

3. Methodology

To generate the link between FE code and ANN, the application of ANN was split into the curve regeneration and interpolation coefficient parts, as shown in Fig. 2. A new curve was generated
from the raw experimental data, and the output was used as an input to the interpolation coefficient part. In both parts, the ANN was trained to learn the relationship between the input and output of nonlinear recovery. To predict the output within a desired range of errors, the number of neurons in the hidden layer was adjusted according to a number of trials. This procedure is discussed further in the next subsection.

3.1. The database and its regeneration

This study utilised the experimental data that have been published by Sun and Wagoner (2011). The published data were chosen based on their comprehensiveness in providing information from the identification of material parameters until the measurements of springback. Fig. 3 shows the tensile test result for a DP980 steel sheet with intermediate unloading cycles. Due to the nonlinear unloading and reloading behaviour, hysteresis loops were formed. These loops are noticeable significantly as the flow stresses increase prior to unloading. Fig. 4(a) shows a magnified view of the fourth cycle from Fig. 3. An $E_{yu}$ of 145 GPa and an $E_p$ of 208 GPa are shown for comparison. It is shown that the current elastic modulus ($E_p$) varied at different stress normalisation points ($\sigma_i/\sigma_0$), where $\sigma_i$ and $\sigma_0$ are given by the current stress and current yield stress. Fig. 4(b) shows the regeneration of the unloading curve by the first ANN, whose architecture is shown in Fig. 5. The true strain and true stress are the input and output of the network.

![Flowchart](image-url)
with eight neurons in the single hidden layer. In both networks, the hyperbolic tangent sigmoid transfer function (tan sigmoid) was chosen as the activation function in the hidden layer due to its ability to learn faster (Haykin, 1999).

3.2. Determination of interpolation coefficient

In the second ANN, the input and output data of the network were formed based on the regenerated curve in Fig. 4(b). An interpolation model was applied to interpolate the range between $E_0$ and $E_{av}$ at every increment $\sigma_1/\sigma_0$, as shown in Eq. (1).

$$C_r = \frac{E_r - E_{av}}{E_0 - E_{av}}$$

where $\sigma_1/\sigma_0$ and $C_r$ are the input and output of the network training. Fig. 6 shows the second ANN architecture with 16 neurons in the single hidden layer. At the end of the second ANN prediction, the weights of the neurons in the network were extracted as matrices. These matrices were then used to establish the ANN link in the FE procedure.

3.3. Establishment of ANN to FE analysis link

The second ANN was completely trained, and the neuron’s weights and biases were extracted in the form of matrices. A feed-forward network from the matrices was implemented into the user-defined material subroutine, as a portion of the material constitutive model used by the FE code in the structural analysis. The feedforward network takes place when the unloading/reloading process occurs after loading in the plastic region. In the FE model, the whole steel sheet was assumed to be a three-dimensional isotropic linearly elastic body (Sun & Wagoner, 2011), and the stress–strain relations are given as:

$$
\begin{align*}
\sigma_x &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\sigma_y &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\sigma_z &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\tau_{xy} &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\tau_{xz} &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\tau_{yz} &= \left[ \lambda + 2\mu \right] \lambda \sigma_0 + \lambda \left( \lambda + 2\mu \right) \lambda \sigma_0 \\
\end{align*}
$$

where the Lamé’s constants $\lambda$ and $\mu$, are related to the modulus of elasticity $E$ and the Poisson’s ratio $\nu$ by:

$$\lambda = \frac{E\nu}{(1 + \nu)(1 - 2\nu)}$$

and

$$\mu = \frac{E}{2(1 + \nu)}$$

In the elastic region, both the unloading and the reloading processes only utilise $E_0$ to determine the stress of the tensor, whereas variation occurs in those processes in the plastic region. As shown in Fig. 4(a), $E_c$ produces a hysteresis loop that lies between $E_0$ and $E_{av}$. Therefore, in FE analysis, $E_c$ need to be updated at every increment of the unloading/reloading process. The function of the feed-forward-network-based constitutive model in an FE model at every increment is as follows:

(i) For the $(i + 1)$th strain increment, the input of the network is the value of $\sigma_1/\sigma_0$. To distinguish the input between unloading and reloading processes, the input is expressed as $\left( 1 - \sigma_1/\sigma_0 \right)$ and $\left( \sigma_1/\sigma_0 \right)$.

(ii) $E_c$ is then calculated by reversing Eq. (1) as:

$$E_c = C_r \times (E_0 - E_{av}) + E_{av}$$

3.4. Draw-bend springback test and simulation

The developed model was then utilised in the simulations of the draw-bend springback test based on the experimental works (Sun & Wagoner, 2011). The published experimental work was chosen based on its capability to represent a wide range of sheet metal forming operations while also having the advantage of simplicity and a controllable sheet tension force. Fig. 7 shows a schematic of the draw-bend test that was utilised to mimic the mechanics in sheet metal forming, which consist of drawing, tensioning, bending, and straightening when passing over the die radius. The strip was cut to a width of 25 mm along the rolling direction, and lubricated with stamping lubricant. There are two hydraulic
4. Results and discussion

The purpose of regenerating the unloading curve was to generalise the determination of the elastic modulus at every $\sigma_i/\sigma_0$, as shown in Fig. 9(a). This determination was used as the training data set for the prediction of $C_e$. If the number of neurons is excessive, the network may generate near perfect matching (over-fitted) of the output to the target, as shown in Fig. 9(a), while the insufficient number of neurons may generate an imprecise unloading curve that affects the accuracy of FE simulation. Fig. 9(b) shows the performance of the network training according to the number of neurons in the hidden layer. Although the mean squared error (MSE) value keeps on decreasing with the increasing number of neurons, the suitable network was found to have eight neurons only. This is due to the consideration of the network architecture of the second ANN that was influenced by the first ANN performance. Fig. 10 shows a comparison of the training data set for the second ANN with respect to the first ANN architecture. A single neuron results in a near straight line, and the increasing number of neurons produce curved data sets. With eight neurons, the network results in quite a smooth curve. However, as the number of neurons increased, the network generates higher fluctuations, which affect the prediction difficulty in the second ANN.

In the interpolation coefficient part, the second ANN architecture was similar to the curve fitting part except for the number of neurons in the hidden layer. In this part, high accuracy is essential as the result was utilised directly in the FE analysis. Therefore, the number of neurons in the hidden layer was chosen to be 8 according to the network performance. Fig. 11(a) shows the performance of the trained network at a various number of neurons. It can be observed that the MSE decreased with the increasing number of neurons and reached a value of $1.75 \times 10^{-5}$ with 16 neurons. This performance is adequate since the training regression reached a value of $0.99998$, as shown in Fig. 11(b).

As shown in Fig. 3, the hysteresis loops are noticeable significantly as the flow stresses increase prior to unloading. This was due to the variation of $E_v$ at each unloading path. Since the network training set was taken from a single hysteresis loop, the interpolation model as shown in Eq. (1) represents its behaviour according to the particular $E_v$, and $E_p$. Therefore, once the model has been trained by the second ANN, its prediction could be used in modelling the unloading process at different initial unloading points.

The establishment of an ANN to FE analysis link utilised the formation of matrix multiplication in the user-material subroutine, where the matrices were the neuron’s weights and biases that were extracted from network training. Therefore, the sizes of the matrices depend on the number of neurons used for the prediction. This consideration was significant as the matrix multiplications were included into the user material subroutine manually. The neurons in the hidden layer calculate the weighted sum of inputs and biases as shown in Eq. (6), and its outputs were passed through the transfer function in Eq. (7) as an input $\left(U_1, U_2, \ldots, U_{16}\right)$ to the output layer.

$$\begin{bmatrix} U_1 \\ U_2 \\ \vdots \\ U_{16} \end{bmatrix} = \text{tanh} \left( \begin{bmatrix} w_{11} \\ w_{12} \\ \vdots \\ w_{16} \end{bmatrix} \left[ \text{Input} \right] + \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_{16} \end{bmatrix} \right)$$

$$\text{tanh}(x) = \frac{2}{1 + e^{-2x}} - 1$$
At the end of the network, the output neuron receives input signals from the hidden layer and computes the weighted sum as shown in Eq. (8), thus producing the final output $C_e$.

$$C_e = [w_{2,1} \quad w_{2,2} \quad \ldots \quad w_{2,16}] \begin{bmatrix} U_1 \\ U_2 \\ \vdots \\ U_{16} \end{bmatrix} + [b_{2,1}]$$  \hspace{1cm} (8)
overall prediction fit obtained was adequate. It is shown that the unloading elastic modulus varied with respect to the plastic pre-strain and the stress normalisation point.

Fig. 14(a)–(c) shows the distribution of the elastic modulus after the springback step. At the end of the springback step, the elastic modulus at the plastically deformed zone experiences significant drop in the elastic modulus, whereas the elastic modulus at both ends of the strip indicates that those regions may be considered as the elastically deformed zone. Furthermore, the elastic modulus varied at different area in the plastically deformed zone. This variation is due to the anticlastic behaviour which contributes to a different normalised stress point for each element after the springback step, which remains as residual stresses. For comparison, Fig. 14(d) shows the distribution of $E_{av}$ for the plastically deformed zone. The uniform distribution of the elastic modulus is the major error contribution to the draw-bend springback test simulation.

Table 1 and Fig. 15 show the results of springback prediction with respect to different types of unloading moduli. All prediction results were compared with the experimental results (Sun & Wagner, 2011), which show that the springback angle of the strip decreases with increasing back force. The standard deviations were calculated as follows:

$$\sigma = \sqrt{\frac{\sum_{i=1}^{N}(\theta_{\text{model}} - \theta_{\text{experiment}})^2}{N}}$$  \hspace{1cm} (9)$$

where $\theta_{\text{model}}$ is the simulated springback angle and $\theta_{\text{experiment}}$ is the angle calculated from the experiment. $N$ is the number of results.
compared and is equal to three. The utilisation of $E_0$ in the unloading process produces under estimation of the springback angle with a standard deviation of 4.68. The springback angles that resulted from the utilisation of $E_{av}$ show a high standard deviation, three times higher than those resulting from $E_0$. On the other hand, the unloading modulus determined by the current model improves the springback prediction as compared to the experimental data.

5. Conclusions

The capability of the developed model to predict the nonlinear unloading for pre-strained steel sheet and the springback of the draw-bend test has been investigated. The applicability of ANN as a part of a constitutive model in FE code has been successfully demonstrated. The application also shows the significance of emphasising the nonlinearity of the unloading modulus instead of the chord modulus, as the final product of springback will result with residual stresses. With an appropriate network architecture, the application has the capability to achieve equivalence to the available experimental data. Therefore, the current work has a high potential to be integrated with the FE software to simulate sheet metal springback phenomenon accurately.

References


Fig. 14. Elastic modulus distribution after springback; for current work (a) left end of the strip, (b) plastically deformed zone, (c) right end of the strip; for chord modulus model, and (d) plastically deformed zone.

Table 1

<table>
<thead>
<tr>
<th>$F_b$</th>
<th>0.3</th>
<th>0.6</th>
<th>0.8</th>
<th>($\phi^0$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Experiment (Sun and Wagoner, 2011)</td>
<td>63.5°</td>
<td>53.9°</td>
<td>45.9°</td>
<td>0</td>
</tr>
<tr>
<td>Current work</td>
<td>66.37°</td>
<td>54.55°</td>
<td>45.94°</td>
<td>1.699</td>
</tr>
<tr>
<td>Initial Young’s modulus</td>
<td>57.7°</td>
<td>49.35°</td>
<td>42.52°</td>
<td>4.6821</td>
</tr>
<tr>
<td>Chord modulus</td>
<td>82.06°</td>
<td>67.66°</td>
<td>58.31°</td>
<td>15.142</td>
</tr>
</tbody>
</table>

Fig. 15. Springback prediction with different types of unloading moduli.


