

Haze Modelling and Simulation in Remote Sensing Satellite Data

Asmala Ahmad

Department of Industrial Computing
Faculty of Information and Communication Technology
Universiti Teknikal Malaysia Melaka
Hang Tuah Jaya, 76100 Durian Tunggal, Melaka, Malaysia

Shaun Quegan

Department of Applied Mathematics
School of Mathematics and Statistics
University of Sheffield
Sheffield, United Kingdom

Copyright © 2014 Asmala Ahmad and Shaun Quegan. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Abstract

In atmospheric haze studies, it is almost impossible to obtain remote sensing data which have the required haze concentration levels. This problem can be overcome if we can generate haze layer based on the properties of real haze to be integrated with remote sensing data. This work aims to generate remote sensing datasets that have been degraded with haze by taking into account the spectral and spatial properties of real haze. Initially, we modelled solar radiances observed from satellite by taking into consideration direct and indirect radiances reflected from the Earth surface during hazy condition. These radiances are then simulated using the 6SV1 radiative transfer model so that the radiances due to haze, or the so called 'haze layer', can be computed. The spatial distribution of the haze layer is simulated based on multivariate Gaussian distribution. The haze layer is finally added to a real dataset to produce a hazy dataset. The generated hazy datasets are to be used in investigating the effects of haze on land cover classification in the future.

Keywords: Haze, Modelling, Simulation, Landsat, Radiance

1 Introduction

Atmospheric aerosols and molecules scatter and absorb solar radiation, thus affecting the downward and upward radiance. Atmospheric scattering and absorption depend substantially on the wavelength of the radiation [16]. Scattering is usually much stronger for short wavelengths than for long wavelengths and significantly affects the classification of surface features [3], [17]. Studies related to haze effects on remote sensing measurements commonly use real hazy datasets [6], [10], [14]. However, acquiring real hazy datasets with a desired range of haze concentrations over an area is almost impossible [1]. A more practical way is to model the haze and simulate its effects on satellite dataset. To do so, we need to know the effects that haze concentrations have on scene visibility and to translate it onto real remote sensing data. An important issue in realising this is to model hazy dataset [16]; in section 2, a model for integrating haze with a clear atmosphere dataset is described. Next, we need to translate the model to practical processes [15]; section 3 discusses radiance calculation using the 6SV1 model. Haze spatial distribution is another key issue in generating real haze [17]; section 4 discusses representation of haze spatial properties using multivariate Gaussian distribution. Finally, the most critical task is to integrate haze layer with a real dataset in order to produce a hazy dataset [12]; section 5 discusses simulation of hazy datasets by incorporating simulated haze path radiance, the effects of signal attenuation and haze spatial distribution onto a clear dataset.

2 Model for Determining Satellite Observed Radiance under Hazy Conditions

The observed radiance, L , that reaches the sensor for a cloudless and haze-free atmosphere can be expressed as [16]:

$$L = L_s + L_D + L_o \quad \dots (1)$$

where L_s is the radiance reflected by the target and directly transmitted through the atmosphere towards the satellite (this gives most information about the target on the Earth's surface), L_D is the radiance reflected from the surface and then scattered by the atmosphere to the sensor (this diffuses radiation between different pixels and thus reduces the spatial variation of the upward radiance), and L_o is the radiance scattered into the sensor's field of view by the atmosphere itself (caused by the atmospheric constituents that exist during clear sky conditions) without reaching the surface - this is independent of surface reflectance and increases

the image brightness. To account for haze, Equation (1) is modified as follows (Figure 1):

$$L = L_S + L_D + L_O + L_H \quad \dots (2)$$

where L_H is the radiance caused by the haze layer. It is independent of the surface reflectance and increases image brightness for dark targets, but decreases it for bright targets. Similarly, Equation (2) can also be expressed as:

$$L = L_S + L_D + (L_O + L_H) = L_S + L_D + L_P \quad \dots (3)$$

where $L_P = L_O + L_H$ is known as path radiance.

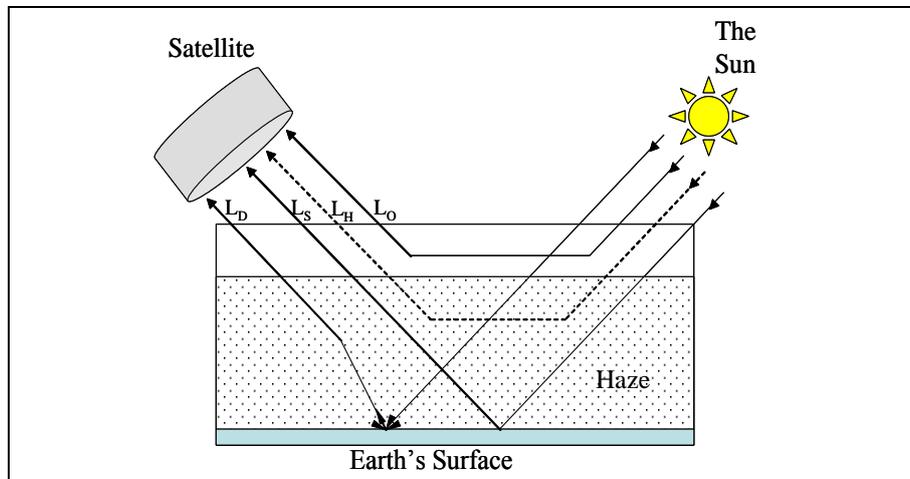


Fig. 1. Modification of the radiance path contributions to the satellite sensor in hazy conditions.

The contribution of L_D is insignificant since it is much weaker than the other components [17] and therefore can be neglected, hence:

$$L \approx L_S + (L_O + L_H) = L_S + L_P \quad \dots (4)$$

We introduce a model for simulation of hazy data in which Equation (4) is written as:

$$L(V) \approx (1 - \beta^{(1)}(V))L_S(\infty) + [L_O + \beta^{(2)}(V)L_H(0)] \quad \dots (5)$$

where $L_S(V) = (1 - \beta^{(1)}(V))L_S(\infty)$ and $L_P(V) = L_O + \beta^{(2)}(V)L_H(0)$. V is the visibility, $L(V)$ is the target radiance at visibility V km, so $L_S(\infty)$ is the radiance

of pure target (i.e. the atmospheric components are assumed insignificant), $L_H(0)$ is for pure haze and the weightings $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ are given by:

$$\beta^{(1)}(V) = 1 - \frac{L_S(V)}{L_S(\infty)} \quad \dots (6)$$

$$\beta^{(2)}(V) = \frac{L_P(V) - L_O}{L_H(0)} \quad \dots (7)$$

In Equation 5, during a clear day, $V = \infty$, $\beta^{(1)}(\infty) = \beta^{(2)}(\infty) = 0$, therefore $L(\infty) = L_S(\infty) + L_O$. For very thick haze, $V = 0$, $\beta^{(1)}(0) = \beta^{(2)}(0) = 1$, so $L(0) = L_O + L_H(0)$. In other words, during clear and very hazy conditions, the radiance observed by the satellite sensor is actually the radiance of true signal and pure haze respectively added with L_O . Between the two extremes, $L_S(V)$ is influenced by $(1 - \beta^{(1)}(V))$ due to atmospheric absorption, while $L_P(V)$ is influenced by $\beta^{(2)}(V)$ due to atmospheric scattering. We can estimate $L_S(\infty)$ from a clear Landsat satellite dataset, while determination of $L_H(0)$, $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ are discussed in the following section.

3 Radiance Calculation Using the 6SV1

6SV1 is the vector version of the 6S (Second Simulation of the Satellite Signal in the Solar Spectrum) [15], [12], though it also works in scalar mode. The vector version is introduced to account for radiation polarisation, due to Rayleigh scattering in a mixed molecular-aerosol atmosphere, which is to be used when performing atmospheric correction [15]. In our study, the 6SV1 is used in simulating haze effects, therefore the radiation polarisation effect is assumed negligible. Hence, our interest is in the scalar mode of 6SV1, which is similar to 6S. 6S makes use of the Successive Order of Scattering (SOS) algorithm to calculate Rayleigh scattering, aerosol scattering and coupling of scattering-absorption. In the SOS, the atmosphere is divided into a number of layers, and the radiative transfer equation is solved for each layer with an iterative approach [12], [15]. In terms of the aerosol model, a refined computation of the radiative properties of basic components (e.g. soot, oceanic, dust-like and water soluble) and additional aerosol components (e.g. stratospheric, desertic and biomass burning) is included. It also has a spectroscopic database for important gases in the 0.25 – 4.0 μm spectrum region, and is able to simulate the TOA signal for both

Lambertian and non-Lambertian targets. For a Lambertian uniform target, the apparent radiance ρ^* is calculated using [12]:

$$\rho^*(\theta_s, \theta_v, \phi_s - \phi_v) = \rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v) + \frac{\rho_t}{1 - \rho_t S} T^\downarrow(\theta_s) T^\uparrow(\theta_v) \quad \dots (8)$$

where $\rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v)$ is the intrinsic atmospheric reflectance associated with aerosol (τ_a) and Rayleigh scattering (τ_r), ρ_t is the surface reflectance, S is the atmospheric spherical albedo, $T^\downarrow(\theta_s)$ is the total downward transmission and $T^\uparrow(\theta_v)$ is the total upward transmission. θ_s and θ_v are the solar and satellite zenith angle respectively and ϕ_s and ϕ_v are solar and satellite azimuth angle respectively.

$$T^\downarrow(\theta_s) = e^{-\tau/\mu_s} + t_d(\theta_s) \quad \dots (9)$$

$$T^\uparrow(\theta_v) = e^{-\tau/\mu_v} + t_d(\theta_v) \quad \dots (10)$$

where $\tau = \tau_a + \tau_r$ is the atmospheric optical thickness associated with aerosol (τ_a) and Rayleigh scattering (τ_r), μ_s and μ_v are $\cos(\theta_s)$ and $\cos(\theta_v)$ respectively and t_d is the diffuse transmittance due to molecules and aerosols. Substituting (10) into (8), we have:

$$\rho^*(\theta_s, \theta_v, \phi_s - \phi_v) = \rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v) + \frac{T^\downarrow(\theta_s)}{1 - \rho_t S} \left(\rho_t e^{-\tau/\mu_v} + \rho_t t_d(\theta_v) \right) \quad \dots (11)$$

For a non-uniform surface:

$$\rho^*(\theta_s, \theta_v, \phi_s - \phi_v) = \rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v) + \frac{T^\downarrow(\theta_s)}{1 - \rho_e S} \left(\rho_t e^{-\tau/\mu_v} + \rho_e t_d(\theta_v) \right) \quad \dots (12)$$

where ρ_e is the environmental reflectance and can be expressed as:

$$\rho_e = \frac{1}{2\pi} \int_0^{2\pi} \int_0^\infty \rho(r, \phi) \frac{dF(r)}{dr} dr d\phi \quad \dots (13)$$

The intrinsic atmospheric reflectance, $\rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v)$, is computed using:

$$\rho_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v) = \rho'_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v) + \left(1 - e^{-\tau/\mu_s}\right) \left(1 - e^{-\tau/\mu_v}\right) \Delta(\tau) \quad \dots (14)$$

where $\rho'_{a+r}(\theta_s, \theta_v, \phi_s - \phi_v)$ is the single-scattering contribution associated with aerosol and molecule scattering and $\left(1 - e^{-\tau/\mu_s}\right) \left(1 - e^{-\tau/\mu_v}\right) \Delta(\tau)$ accounts for higher orders of scattering. The atmospheric spherical albedo S is calculated using:

$$S = \frac{1}{4 + 3\tau} \left[3\tau - 4E_3(\tau) + 6E_4(\tau) \right] \quad \dots (15)$$

where $E_3(\tau)$ and $E_4(\tau)$ are exponential integrals depending on τ . To exploit Equation (5), we need to determine $L_H(0)$, $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$. To do so, we use the 6SV1 code to calculate satellite apparent radiance, path radiance, signal radiance and diffuse radiance, for bands 1, 2, 3, 4, 5, and 7 of the Landsat satellite. The atmospheric and aerosol model used were Tropical Model and Biomass Burning respectively. The latter accounts for haze that originates from forest fires. Initially, visibility was varied from 0.5 to 100 km, but later only visibilities from 0.5 to 20 km were taken into account. The following section further explains this issue. Figure 2 shows satellite apparent radiance, path radiance, signal radiance and diffuse radiance as a function of visibility. It is obvious that for bands 1, 2 and 3, the path radiance is higher than the diffuse radiance at all visibilities. For bands 4, 5 and 7, the path and diffuse radiance are about the same but the signal radiance is comparatively much higher. This shows that at shorter wavelengths the haze effects are significant and dominated by the path radiance; while at longer wavelengths, the haze effects are almost negligible due to the much higher signal radiance. It is also observed that the major impact on the radiances occurs for visibilities less than 20 km. Hence, we make the approximations $L_S(\infty) \approx L_S(20)$ and $L_P(\infty) = L_O \approx L_P(20)$. Also, in 6SV1, calculations cannot be made for visibilities less than 0.5 km, so we assume $L_S(0) \approx L_S(0.5)$ and $L_P(0) \approx L_P(0.5) = L_O + L_H(0.5)$. Thus, Equation 5 can be written as:

$$L(V) \approx \left(1 - \beta^{(1)}(V)\right) L_S(20) + \left[L_O + \beta^{(2)}(V) L_H(0.5) \right] \quad \dots (16)$$

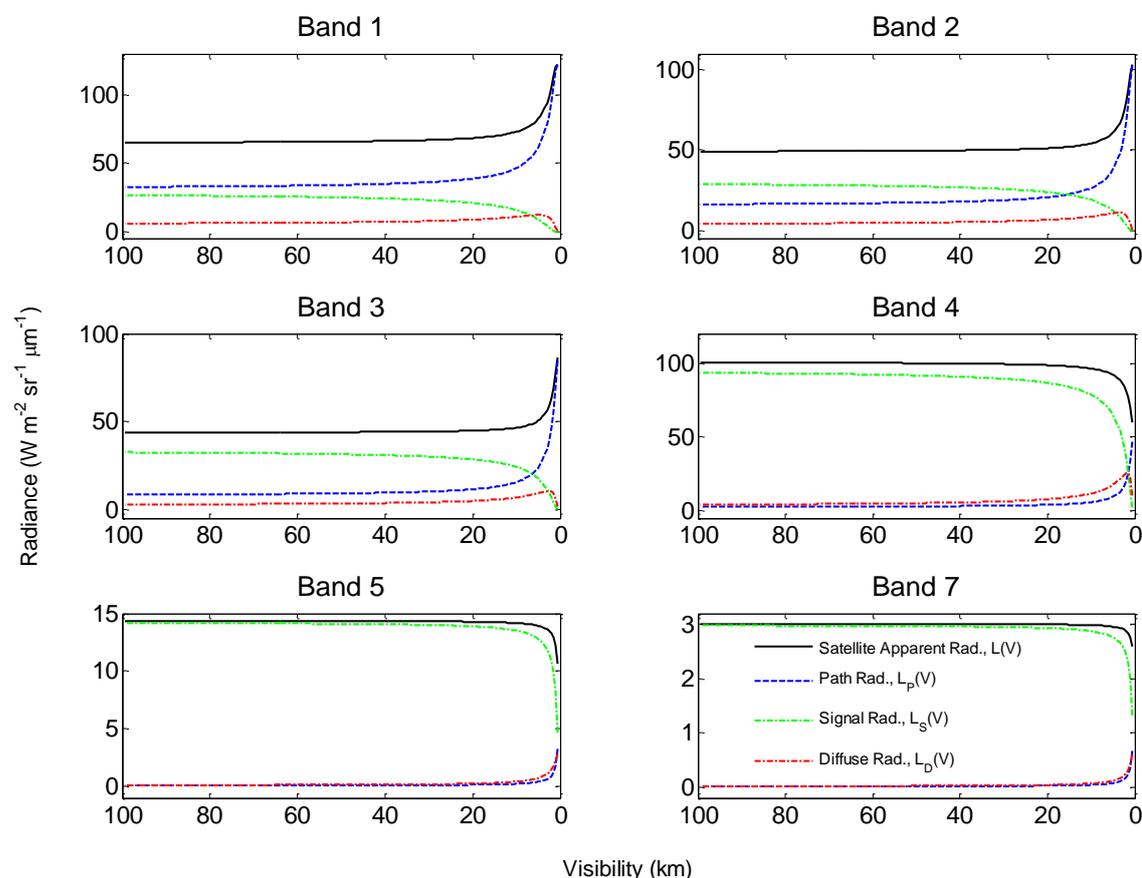


Fig. 2. Satellite apparent radiance, path radiance, signal radiance and diffuse radiance as a function of visibility as visibility runs from 0.5 to 100 km.

Determination of the Weightings, $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$

Calculation of $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ is carried out using:

$$\beta^{(1)}(V) = 1 - \frac{L_s(V)}{L_s(20)} \quad \dots (17)$$

$$\beta^{(2)}(V) = \frac{L_p(V) - L_o}{L_H(0.5)} \quad \dots (18)$$

Plots of $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ against visibility for bands 1, 2, 3, 4, 5 and 7 are shown in Figure 3. The difference between $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ is due to the

difference between the true signal attenuation and the pure haze weighting, which is more obvious in shorter (i.e. lower-numbered bands) than longer wavelengths (i.e. higher-numbered bands). $\beta^{(1)}(V)$ is higher than $\beta^{(2)}(V)$ for shorter wavelengths but this is not the case for longer wavelengths. For shorter wavelengths, $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ show a small difference at longer visibilities. The difference increases as visibility decreases to about 4 km, but then decreases towards 0 km. For longer wavelengths, the difference is only obvious at very short visibilities. At very long visibilities, the difference is not significant, hence use of a single weighting can be considered for these visibilities. Nevertheless, to account for the entire visibilities, the use of different weightings is appropriate due to the inconsistency between the signal attenuation and haze weighting, particularly at moderate and longer visibilities.

Simulation of the Haze Radiance Component, $\beta^{(2)}(V)L_H(0)$

The interaction between solar radiation and the haze constituents affects the spectral measurements made from a satellite remote sensing system and degrades the quality of the images, for example by reducing the contrast between objects and ultimately making them inseparable. Statistically, for a single spectral measurement, haze modifies the mean and standard deviation, but, in a multispectral system the covariance structure of the multispectral measurements is also affected. These effects need to be simulated when using Equation 5 to model haze observed in multispectral Landsat data. We assume that haze can be treated as a random noise that can be modelled as a multivariate Gaussian random variable with mean $\boldsymbol{\mu}$ (haze radiance) and covariance matrix C (covariance structure of haze observed by Landsat).

4 Representation of Haze Spatial Properties using Multivariate Normal Distribution

In simulating haze in remote sensing dataset, we need to take into account its spatial distribution and spectral correlation. In practice, these parameters are difficult to measure due to dynamic behaviour of haze. Here, we assume haze to be spatially uncorrelated, so that it can sensibly simulate haze effects. If the haze was to be spatially correlated, it will appear as patches with high spatial correlation, which are unlikely to represent a real haze condition. Hence, haze can be modelled with an N-dimensional Gaussian probability density function which has the form:

$$P(\mathbf{X}) = (2\pi)^{-\frac{N}{2}} (|C|)^{-\frac{1}{2}} \exp\left(-\frac{1}{2}(\mathbf{X}-\boldsymbol{\mu})^t C^{-1}(\mathbf{X}-\boldsymbol{\mu})\right) \quad \dots (19)$$

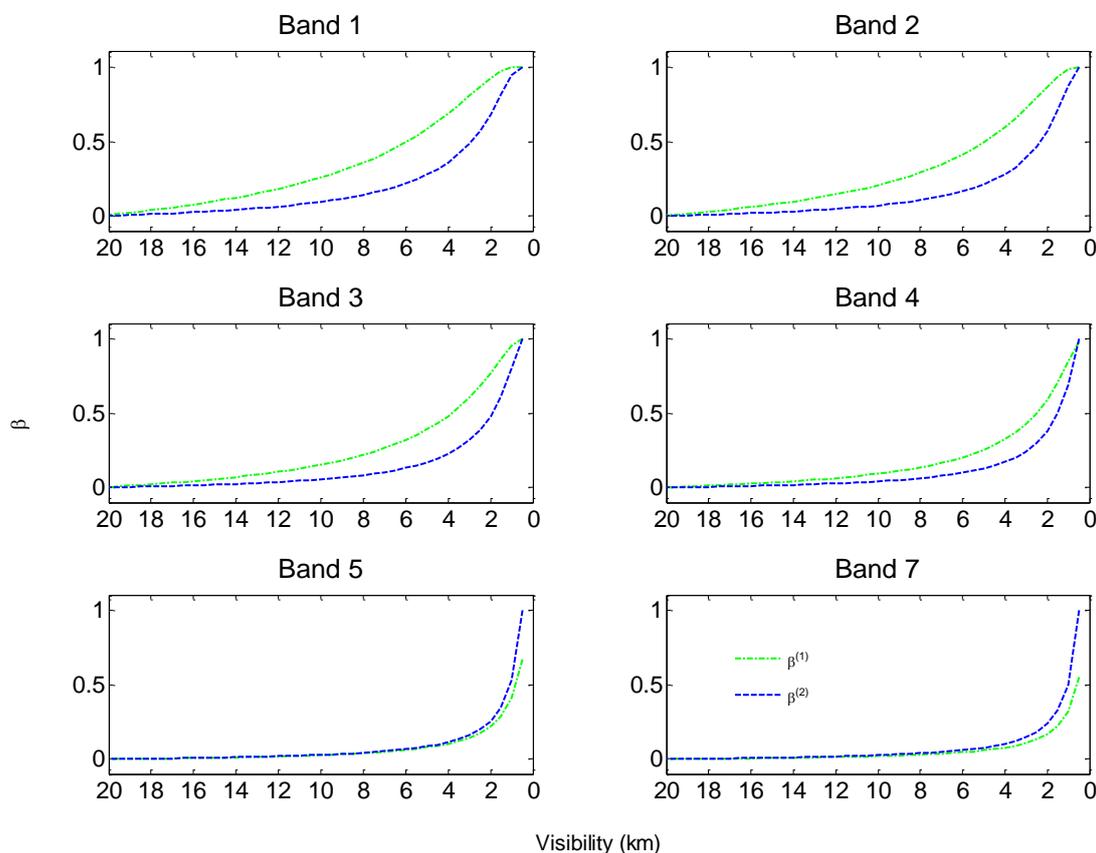


Fig. 3. Plots of $\beta^{(1)}(V)$ and $\beta^{(2)}(V)$ against visibility.

where \mathbf{X} is an N -dimensional random variable representing the N Landsat bands, i.e. the observed haze, $\boldsymbol{\mu}$ is the vector of means and \mathbf{C} is the $N \times N$ covariance matrix. In order to use this model, we need estimation of $\boldsymbol{\mu}$ and \mathbf{C} . We set $\boldsymbol{\mu} = \beta^{(2)}(V) \mathbf{L}_H(0.5)$ where $\mathbf{L}_H(0.5)$ is obtained from the atmospheric haze radiance for 0.5 km visibility, calculated using 6SV1. Since haze is usually considered as thin cloud in satellite spectral measurements [4], [7], [9], [11], [13], [18], the covariance, \mathbf{C} , is measured using observations of cloud in Landsat bands 1, 2, 3, 4, 5 and 7 from 11 February 1999, as given in Table 1. There is quite a strong correlation between bands, especially amongst band 1, 2 and 3 as well as between band 5 and 7, due to their similar spectral measurement properties. The covariance will play an important role in simulating the effects of haze on land cover classification [8], [2], [5]. 11 sets of haze layers, representing 11 different visibilities, were then generated, where each layer consists of 758 x 792 pixels, which is the same size as the clear dataset.

Table 1: Cloud covariances (along and above the diagonal) and correlations (below the diagonal) calculated from Landsat bands 1, 2, 3, 4, 5 and 7.

| Band | 1 | 2 | 3 | 4 | 5 | 7 |
|------|--------|---------|---------|---------|--------|-------|
| 1 | 432.74 | 771.38 | 706.31 | 440.36 | 84.73 | 29.59 |
| 2 | 0.80 | 2147.19 | 1872.28 | 1255.49 | 225.26 | 90.50 |
| 3 | 0.83 | 0.98 | 1692.62 | 1103.61 | 207.53 | 84.07 |
| 4 | 0.71 | 0.91 | 0.90 | 879.83 | 154.98 | 59.97 |
| 5 | 0.68 | 0.81 | 0.85 | 0.88 | 35.63 | 14.64 |
| 7 | 0.53 | 0.72 | 0.76 | 0.75 | 0.91 | 7.31 |

5 Simulation of a Hazy Dataset

The haze component is assumed to be independent of the signal component, so the hazy dataset can be synthesised by adding a weighted pure haze, $\beta^{(2)}(\mathbf{V})L_H(0.5)$ to the weighted true signal $(1-\beta^{(1)}(\mathbf{V}))L_S(20)+L_O$. Here, the true signal component is estimated from Landsat-5 TM dataset (from 11 February 1999 with 20 km visibility, based on the average of 6 stations within 5 to 60 km from the centre of the scene, i.e. Klang Port, Petaling Jaya, Sepang, Serdang, Tanjung Karang and Banting. Based on Equation (16) and for simplicity, we define $T_i = L_S(20)$ and $H_i = L_H(0.5)$. Consequently, due to the vector-based structure of a dataset, the hazy dataset, $L_i(\mathbf{V})$ can be written as:

$$L_i(\mathbf{V}) = (1 - \beta_i^{(1)}(\mathbf{V}))T_i + L_O + \beta_i^{(2)}(\mathbf{V})H_i \quad \dots (20)$$

An example of hazy dataset simulation for 4 km visibility is shown in Figure 4. The model components, the simulated hazy band 1 and the corresponding histogram are shown in the left, middle and right column respectively. It can be seen that the histogram of the hazy scene has been modified due to haze. The histogram seems to be in a form of normal distribution but skewed to left, i.e. some characteristics from the original scene are still preserved. Hazy scenes were generated for 11 visibilities (20, 18, 16, 14, 12, 10, 8, 6, 4, 2 and 0 km) and six Landsat bands (band 1, 2, 3, 4, 5 and 7). These datasets can be used in the future to investigate the effects of haze on land cover classification.

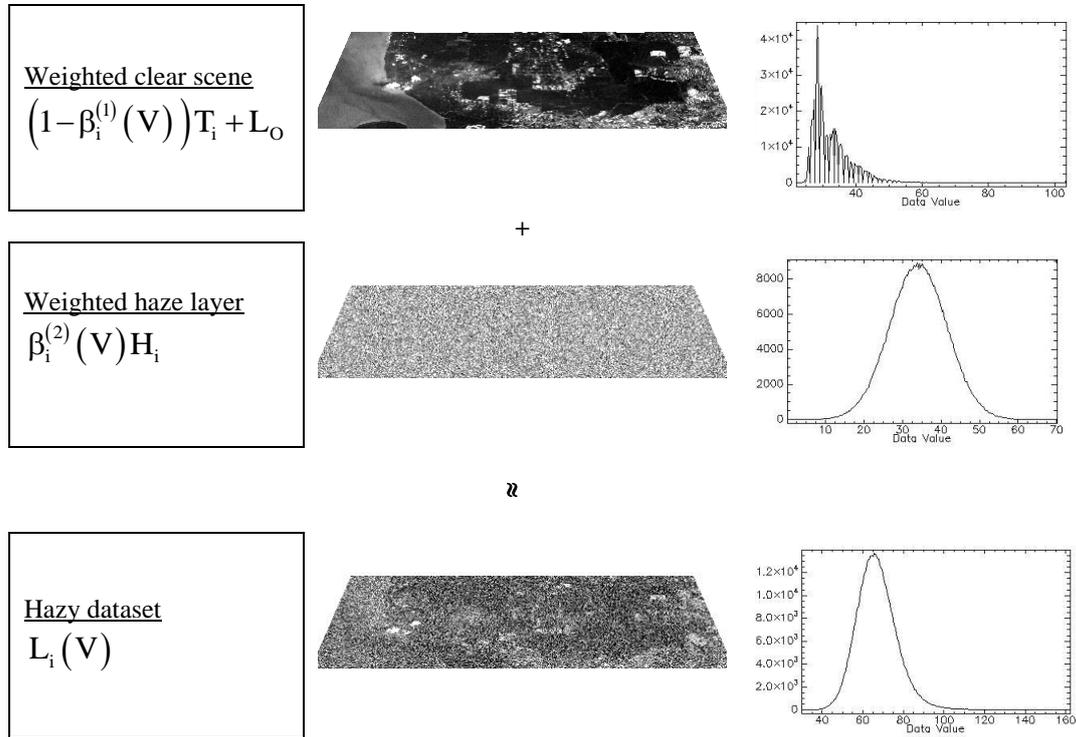


Fig. 4. Process of integrating a hazy layer with a clear data from band 1 to produce a 4 km ($V = 4$) visibility hazy dataset.

6 Conclusion

In this study, we successfully modelled and simulated haze layers to produced hazy datasets. Spectral and spatial properties of haze are required in order to simulate the haze layers. The spectral properties come from atmospheric path radiance that is simulated using the 6SV1 radiative transfer model. The spatial properties are simulated using 6-dimensional Gaussian probability density function that made use the cloud covariance. The hazy datasets are to be used in studying haze effects on land cover classification in remote sensing data.

Acknowledgments. We thank Universiti Teknikal Malaysia Melaka (UTeM) for funding this study under UTeM PJP Grant (PJP/2013/FTMK (4A)/S01146).

References

- [1] A. Ahmad and M. Hashim, Determination of haze using NOAA-14 satellite data, Proceedings on The 23rd Asian Conference on Remote Sensing 2002 (ACRS 2002), (2012), in cd.
- [2] A. Ahmad and S. Quegan, Analysis of maximum likelihood classification on multispectral data, Applied Mathematical Sciences, 6 (2012), 6425 – 6436.
- [3] A. Ahmad and S. Quegan, Analysis of maximum likelihood classification technique on Landsat 5 TM satellite data of tropical land covers, Proceedings of 2012 IEEE International Conference on Control System, Computing and Engineering (ICCSCE2012), (2012), 1 – 6.
<http://dx.doi.org/10.1109/iccsce.2012.6487156>
- [4] A. Ahmad and S. Quegan, Cloud masking for remotely sensed data using spectral and principal components analysis, Engineering, Technology & Applied Science Research (ETASR), 2 (2012), 221 – 225.
- [5] A. Ahmad and S. Quegan, Comparative analysis of supervised and unsupervised classification on multispectral data, Applied Mathematical Sciences, 7 (74) (2013), 3681 – 3694.
<http://dx.doi.org/10.12988/ams.2013.34214>
- [6] A. Ahmad and S. Quegan, Haze reduction in remotely sensed data. Applied Mathematical Sciences, 8 (36) (2014), 1755 – 1762.
<http://dx.doi.org/10.12988/ams.2014.4289>
- [7] A. Ahmad and S. Quegan, Multitemporal cloud detection and masking using MODIS data, Applied Mathematical Sciences, 8 (7) (2014), 345 – 353.
<http://dx.doi.org/10.12988/ams.2014.311619>
- [8] A. Ahmad, Analysis of Landsat 5 TM data of Malaysian land covers using ISODATA clustering technique, Proceedings of the 2012 IEEE Asia-Pacific Conference on Applied Electromagnetic (APACE 2012), (2012), 92 – 97.
<http://dx.doi.org/10.1109/apace.2012.6457639>
- [9] A. Ahmad, B. M. Aboobaidar and N. M. Hashim, A Localised cloud detection and masking method using spectral analysis, Australian Journal of Basic and Applied Sciences 7 (14), 3 - 10.

- [10] A. Asmala, M. Hashim, M. N. Hashim, M. N. Ayof and A. S. Budi, The use of remote sensing and GIS to estimate Air Quality Index (AQI) Over Peninsular Malaysia, *GIS development*, (2006), 5pp.
- [11] C. Y. Ji, Haze reduction from the visible bands of LANDSAT TM and ETM+ images over a shallow water reef environment, *Remote Sensing of Environment*, 112 (2008), 1773 – 1783.
<http://dx.doi.org/10.1016/j.rse.2007.09.006>
- [12] E. F. Vermote, D. Tanre, Deuze, M. Herman and J. Morcrette, Second simulation of the satellite signal in the solar spectrum, 6S: An overview, *IEEE Transactions on Geoscience and Remote Sensing*, 35 (1997), 675 – 686. <http://dx.doi.org/10.1109/36.581987>
- [13] G. D. Moro and L. Halounova, Haze removal for high-resolution satellite data: a case study. *International Journal on Remote Sensing*, 28 (10) (2007), 2187 – 2205. <http://dx.doi.org/10.1080/01431160600928559>
- [14] M. Hashim, K. D. Kanniah, A. Ahmad, A. W. Rasib, Remote sensing of tropospheric pollutants originating from 1997 forest fire in Southeast Asia, *Asian Journal of Geoinformatics* 4, 57 – 68.
- [15] S. Y. Kotchenova, E. F. Vermote, R. Matarrese and F. J. Klemm Jr., Validation of a vector version of the 6S radiative transfer code for atmospheric correction of satellite data. Part I: Path Radiance, *Applied Optics*, 45 (26) 2006, 6726 – 6774. <http://dx.doi.org/10.1364/ao.45.006762>
- [16] Y. J. Kaufman and C. Sendra, Algorithm for automatic atmospheric corrections to visible and near-IR satellite imagery, *International Journal on Remote Sensing*, 9 (8) (1988), 1357 – 1381.
<http://dx.doi.org/10.1080/01431168808954942>
- [17] Y. J. Kaufman and R. S. Fraser, Different atmospheric effects in remote sensing of uniform and nonuniform surfaces, *Advances in Space Research*, 2 (5) (1983), 147 – 155. [http://dx.doi.org/10.1016/0273-1177\(82\)90342-8](http://dx.doi.org/10.1016/0273-1177(82)90342-8)
- [18] Y. Zhang, B. Guindon and J. Cihlar, An image transform to characterize and compensate for spatial variations in thin cloud contamination of Landsat images. *Remote Sensing of Environment*, 82 (2002), 173 – 187.
[http://dx.doi.org/10.1016/s0034-4257\(02\)00034-2](http://dx.doi.org/10.1016/s0034-4257(02)00034-2)

Received: September 29, 2014; Published: November 14, 2014